PSC 202
SYRACUSE UNIVERSITY
INTRODUCTION TO POLITICAL
ANALYSIS
MORE HYPOTHESIS TESTING WITH ONE CONFOUNDER

## HOUSEKEEPING

- No in-person sections on Friday
- Instead, we will distribute a worksheet to complete at your leisure
- Due December 1 (Friday in 2 weeks)
- Graded pass/fail, counts towards section attendance/participation
- If you have questions about the material, please email and/or attend student hours


## HOUSEKEEPING

- Problem Set 8 will be posted this week - Also due December 1


## LAST TIME

Partisanship



## Feeling safer if more armed security

## PARTISANSHIP \& SAFETY



## MAYBE THIS IS GOING ON?

Non-white students more likely to be Democrats than white students


Partisanship (X)

Race (Z)
Non-white students more likely to not feel safer with
armed security than white students

Feeling safer if more armed security (Y)

Partisanship by itself has no effect on feeling safer

## POTENTIAL CONCERN

Disproportionately non-white students

|  | Democrats | Not Democrats |
| :---: | :---: | :---: | Total

## MAYBE THIS IS GOING ON?

Non-white students more likely to be Democrats than white students


Partisanship (X) Race (Z)

Non-white students more likely to not feel safer with
armed security than white students

Feeling safer if more armed security (Y)

- How can we find out if this is what's going on?


## CONTROLLED COMPARISON TABLE

| White |  |  |  |  | Non-White |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | Dem | NonDem | Total | Dem | $\begin{aligned} & \text { Non- } \\ & \text { Dem } \end{aligned}$ | Total |
| Feel Safer Not Feel Safer |  |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  |
|  | Total |  |  |  |  |  |  |

## CONTROLLED COMPARISON TABLE

|  |  | White |  |  | Non-White |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| ָ̄凶 |  | Dem | NonDem | Total | Dem | Non- Dem | Total |
|  | $\begin{aligned} & \text { Feel } \\ & \text { Safer } \end{aligned}$ | $\begin{aligned} & 42 \% \\ & (15) \end{aligned}$ | $\begin{aligned} & 61 \% \\ & (11) \end{aligned}$ | $\begin{gathered} 48 \% \\ (26) \end{gathered}$ |  |  |  |
| $\begin{aligned} & \text { ¿ } \\ & \end{aligned}$ | Not Feel Safer | $\begin{gathered} 58 \% \\ (21) \end{gathered}$ | $39 \%$ (7) | $\begin{gathered} 52 \% \\ (28) \end{gathered}$ |  |  |  |
| $\Sigma$ | Total | $\begin{gathered} 100 \% \\ (36) \end{gathered}$ | $\begin{gathered} 100 \% \\ (18) \end{gathered}$ | $\begin{gathered} 100 \% \\ (54) \end{gathered}$ |  |  |  |

## CONTROLLED COMPARISON TABLE

|  | White |  |  |  | Non-White |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | ${ }_{15}$ | $\begin{gathered} \text { Non- } \\ \% \text { Pem } \end{gathered}$ | Total | Dem | Non- Dem | Total |
| O | Feel | 42\% | 61\% | 48\% |  |  |  |
| $\stackrel{\oplus}{\natural}$ | Safer | (15) | (11) | (26) |  |  |  |
| ¢ | Not Feel Safer | $\begin{aligned} & 58 \% \\ & (21) \end{aligned}$ | 39\% | $52 \%$ |  |  |  |
| ${ }^{\circ}$ | Total | $\begin{gathered} 100 \% \\ (36) \end{gathered}$ | $\begin{aligned} & 100 \% \\ & (18) \end{aligned}$ | $\begin{gathered} 100 \% \\ (54) \end{gathered}$ |  |  |  |

## PARTISANSHIP \& VACCINATION

- Among white students, Democrats are less likely to feel safer with armed security than Non-Democrats
- White Democrats 19 percentage points less likely to report feeling safer than white non-Democrats


## TERMINOLOGY

- Controlled effect: relationship between an independent variable ( X ) and a dependent variable ( Y ) within one value of another independent variable (Z)
- e.g. relation between partisanship ( X ) and feeling safer ( Y ) among white students (one value of Z )

| White |  |  |  | Non-White |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | Dem |  | Total | Dem | Non- <br> Dem | Total |
| Feel | 42\% | 61\% | 48\% | 40\% | 54\% | 45\% |
| Safer | (15) | (11) | (26) | (8) | (7) | (15) |
| Not Feel Safer | $\begin{gathered} 58 \% \\ (21) \end{gathered}$ | $39 \%$ <br> (7) | $\begin{gathered} 52 \% \\ (28) \end{gathered}$ | $\begin{gathered} 60 \% \\ (12) \end{gathered}$ | $46 \%$ <br> (6) | 55\% <br> (18) |
| Total | $100 \%$ (36) | $100 \%$ | $100 \%$ (54) | $\begin{gathered} 100 \% \\ (20) \end{gathered}$ | $100 \%$ (13) | $100 \%$ (33) |


| White |  |  |  | Non-White |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | Dem |  | Total | Dem 14 |  | Total |
| Feel | 42\% | 61\% | 48\% | 40\% | 54\% | 45\% |
| Safer | (15) | (11) | (26) | (8) | (7) | (15) |
| Not Feel Safer | $\begin{gathered} 58 \% \\ (21) \end{gathered}$ | $39 \%$ <br> (7) | $\begin{gathered} 52 \% \\ (28) \end{gathered}$ | $\begin{gathered} 60 \% \\ (12) \end{gathered}$ | 46\% <br> (6) | 55\% <br> (18) |
| Total | $100 \%$ (36) | $100 \%$ (18) | $100 \%$ (54) | $100 \%$ (20) | $100 \%$ (13) | $100 \%$ (33) |

## PARTISANSHIP \& VACCINES

- Among non-white students, Democrats are less likely to feel safer with armed security than Non-Democrats
- Non-white Democrats 14 percentage points less likely to report feeling safer than non-white nonDemocrats


## PARTISANSHIP \& VOTING

- So even if we take race into account, partisanship still has effect on safety feelings
- Among both white and non-white students,

Democrats less likely to feel safer

- Partial relationship/partial effect: relationship between two variables after taking effect of other variables into account
- e.g. relation between partisanship and safety feeling, controlling for race
- Partial relationship summarizes the controlled effects


## HOW DOES THIS HELP?

- Is there a credible causal mechanism that connects X to Y ?
- Can we rule out the possibility that Y could cause X ?
- Is there covariation between $X$ and $Y$ ?
- Have we controlled for all confounding variables ( $Z$ ) that might make the association between $X$ and $Y$ spurious?


## HOW DOES THIS HELP?

- Logic of control
- What is the relationship between $X$ and $Y$ when we control for one confounder?
- Ultimate goal: What is the relationship between $X$ and $Y$ when we control for many confounders?


## PARTISANSHIP \& GUN CONTROL

## Partisanship (X)



## Support for gun control (Y)

## PARTISANSHIP \& GUN CONTROL

|  | Democrats | Republicans | Total |
| :---: | :---: | :---: | :---: |
| Stricter Gun | $58 \%$ <br> Control | $42 \%$ <br> $(7)$ | $50 \%$ <br> $(12)$ |
| Not Stricter | $42 \%$ <br> Gun Control | $58 \%$ <br> $(5)$ | $50 \%$ <br> $(7)$ |
| Total | $100 \%$ <br> $(12)$ | $100 \%$ <br> $(12)$ | $100 \%$ <br> $(24)$ |

- Hypothetical example


## ZERO-ORDER EFFECT

|  | Democrat | Republicans | Total |
| :---: | :---: | :---: | :---: |
| Stricter Gun Control | 58\% | 42\% | $\begin{aligned} & 50 \% \\ & \text { (12) } \end{aligned}$ |
|  | (7) | (5) |  |
| Not Stricter | 42\% | 58\% | 50\% |
| Gun Control | (5) | (7) | (12) |
| Total | $\begin{gathered} 100 \% \\ (12) \end{gathered}$ | $\begin{aligned} & 100 \% \\ & (12) \end{aligned}$ | $\begin{gathered} 100 \% \\ (24) \end{gathered}$ |

## CONFOUNDER?

W are more likely than M to be Democrats

## Partisanship (X)

## Gender (Z)

W are more likely than $M$ to support gun control


Support for gun control (Y)

Partisanship by itself has no effect on support for gun control

## PARTISANSHIP \& GUN CONTROL

Female
Male

|  | Dem | Rep | Total | Dem | Rep |
| :--- | :--- | :--- | :--- | :--- | :--- |
| Stricter <br> Gun <br> Control <br> Not |  |  |  |  |  |
| Stricter <br> Gun |  |  |  |  |  |
| Total |  |  |  |  |  |

## PARTISANSHIP \& GUN CONTROL

Female

|  | Dem | Rep | Total | Dem | Rep | Total |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Stricter <br> Gun <br> Control | $75 \%$ <br> $(6)$ | $75 \%$ <br> $(3)$ | $75 \%$ <br> (9) |  |  |  |
| Not <br> Stricter <br> Gun | $25 \%$ <br> $(2)$ | $25 \%$ <br> $(1)$ | $25 \%$ <br> $(3)$ |  |  |  |
| Total | $100 \%$ <br> $(8)$ | $100 \%$ <br> $(4)$ | $100 \%$ <br> $(12)$ |  |  |  |
|  |  |  |  |  |  |  |

## PARTISANSHIP \& GUN CONTROL

Female

|  | Dem | Rep | Total | Dem | Rep | Total |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Stricter Gun Contro | $75 \%$ <br> (6) | $75 \%$ <br> (3) | $75 \%$ <br> (9) | 25\% <br> (1) | 25\% <br> (2) | $25 \%$ <br> (3) |
| Not Stricter Gun | $25 \%$ <br> (2) | 25\% <br> (1) | 25\% <br> (3) | 75\% <br> (3) | 75\% <br> (6) | $75 \%$ <br> (9) |
| Total | 100\% (8) | 100\% <br> (4) | 100\% <br> (12) | 100\% <br> (4) | 100\% <br> (8) | 100\% <br> (12) |

## PARTISANSHIP \& GUN CONTROL

|  | Female |  |  | Male |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | $0 \%$ |  | Total | $0 \%$ |  | Total |
| Stricter | 75\% | 75\% | 75\% | 25\% | 25\% | 25\% |
| Control | (6) | (3) | (9) | (1) | (2) | (3) |
| Not Stricter Gun | 25\% <br> (2) | 25\% <br> (1) | 25\% <br> (3) | 75\% <br> (3) | 75\% <br> (6) | $\begin{gathered} 75 \% \\ \text { (9) } \end{gathered}$ |
| Total | $100 \%$ <br> (8) | 100\% <br> (4) | $100 \%$ (12) | $100 \%$ <br> (4) | $100 \%$ <br> (8) | $100 \%$ (12) |

- Partial effect of partisanship, "controlling for" gender


## SPURIOUS RELATIONSHIP

## Gender (Z)



Partisanship (X)


- Relation between partisanship and support for gun control was spurious
- Caused by compositional differences
- Once we "control for" gender, no independent effect of partisanship


## A DIFFERENT EXAMPLE

|  | Female |  |  | Male |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | Dem | Rep | Total | Dem | Rep | Total |
| Stricter Gun Control | 66\% <br> (4) | 50\% <br> (3) | 58\% <br> (7) | 33\% <br> (2) | 17\% <br> (1) | 25\% <br> (3) |
| Not Stricter Gun | 33\% <br> (2) | 50\% <br> (3) | 42\% <br> (5) | 66\% <br> (4) | 83\% <br> (5) | $\begin{gathered} 75 \% \\ \text { (9) } \end{gathered}$ |
| Total | $100 \%$ <br> (6) | $100 \%$ <br> (6) | $100 \%$ (12) | 100\% <br> (6) | $100 \%$ <br> (6) | $100 \%$ (12) |

- What are the controlled effects?


## PARTIAL EFFECTS

|  | Female |  |  | Male |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | Dem | Rep \% | Total | Dem 1 | Rep | Total |
| Stricter Gun | 66\% | 50\% | $58 \%$ | 33\% | 17\% | 25\% <br> (3) |
| Control | (4) | (3) |  | (2) | (1) |  |
| Not Stricter Gun | $33 \%$ (2) | 50\% <br> (3) | 42\% <br> (5) | 66\% <br> (4) | 83\% <br> (5) | 75\% (9) |
| Total | 100\% <br> (6) | $100 \%$ <br> (6) | $100 \%$ (12) | 100\% <br> (6) | 100\% <br> (6) | $100 \%$ (12) |

## WHAT WE FIND...

- Partisanship still has an independent effect on attitudes among both men and women


## ADDITIVE RELATIONSHIP

## Gender (Z)

## Partisanship (X)



## Support for gun control (Y)

- Both partisanship and gender determine gun control attitudes


## YET ANOTHER EXAMPLE

## Female

|  | Dem | Rep | Total | Dem | Rep | Total |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Stricter | $57 \%$ | $50 \%$ | $55 \%$ | $60 \%$ | $38 \%$ | $46 \%$ |
| Gun <br> Control | (4) <br> $(2)$ | $(6)$ | $(3)$ | $(3)$ | $(6)$ |  |
| Not <br> Stricter <br> Gun | $43 \%$ | $50 \%$ | $45 \%$ | $40 \%$ | $62 \%$ | $54 \%$ |
| (3) | $(2)$ | $(5)$ | $(2)$ | $(5)$ | $(7)$ |  |
| Total | $100 \%$ | $100 \%$ | $100 \%$ | $100 \%$ | $100 \%$ | $100 \%$ |
|  | $(7)$ | $(4)$ | $(11)$ | $(5)$ | $(8)$ | $(13)$ |

## PARTIAL EFFECTS

Female
Male

|  | $7 \%$ |  | Total | Dem 22 | $\% \text { Rep }$ | Total |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Stricter | 57\% | 50\% | 55\% | 60\% | 38\% | 46\% |
| Gun Control | (4) | (2) | (6) | (3) | (3) | (6) |
| Not Stricter Gun | 43\% <br> (3) | 50\% <br> (2) | 45\% <br> (5) | 40\% <br> (2) | 62\% <br> (5) | 54\% <br> (7) |
| Total | 100\% <br> (7) | $100 \%$ <br> (4) | $\begin{gathered} 100 \% \\ (11) \end{gathered}$ | $100 \%$ <br> (5) | $100 \%$ <br> (8) | $100 \%$ (13) |

- Partisanship still has an independent effect on attitudes among both men and women
- But these effects are of different size!
- The effect of partisanship is stronger among men than among women


## WHAT WE FIND...

## Female

|  | Dem | Rep | Total | $\text { Dem } 22 \%$ |  | Total |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Stricter | 57\% | 50\% | 55\% | 60\% | 38\% | 46\% |
| Control | (4) | (2) | (6) | (3) | (3) | (6) |
| Not Stricter Gun | 43\% <br> (3) | 50\% <br> (2) | 45\% <br> (5) | 40\% <br> (2) | 62\% <br> (5) | 54\% <br> (7) |
| Total | 100\% <br> (7) | $100 \%$ <br> (4) | 100\% <br> (11) | $100 \%$ <br> (5) | $100 \%$ <br> (8) | 100\% <br> (13) |

## INTERACTIVE RELATIONSHIP



- Gender determines how much partisanship affects gun control attitudes


## WHAT HAVE WE LEARNED?

- Want to know: Is there an effect of X on Y ?
- Zero-order relationship not 0? Great!
- But what about Z?
- Learned: How to check if $X$ has an independent effect on $Y$, controlling for $\mathbf{Z}$
- Spurious relationship
- Additive relationship
- Interactive relationship
- How can we tell whether a relation is spurious, additive, or interactive?


## HOW CAN WE TELL WHICH ONE?

1. Are all controlled/partial effects zero or very close to zero?

- Yes? $\Rightarrow$ relationship between x and y is spurious
- No? $\Rightarrow$ either additive or interactive

2. Are all controlled/partial effects approximately the same size?

- Yes? $\Rightarrow$ additive relationship
- No? = interactive relationship


## BACK TO OUR SURVEY

| White |  |  |  | Non-White |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | Dem | $\begin{aligned} & \text { Non- } \\ & \%{ }^{\text {Dem }} \end{aligned}$ | Total | Dem $\qquad$ | $\begin{aligned} & \text { Non- } \\ & \%^{\text {Dem }} \\ & \hline \hline \end{aligned}$ | Total |
| Feel | 42\% | 61\% | 48\% | 40\% | 54\% | 45\% |
| Safer | (15) | (11) | (26) | (8) | (7) | (15) |
| Not Feel Safer | 58\% <br> (21) | 39\% <br> (7) | 52\% <br> (28) | 60\% <br> (12) | 46\% <br> (6) | 55\% <br> (18) |
| Total | 100\% (36) | 100\% (18) | 100\% (54) | 100\% (20) | $100 \%$ (13) | $100 \%$ (33) |

- Partial effect of partisanship, "controlling for" race


## HOW CAN WE TELL WHICH ONE?

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2. Are all controlled/partial effects approximately the same size?

- Yes? $\Rightarrow$ additive relationship
- No? $\Rightarrow$ interactive relationship


## BACK TO OUR SURVEY

| White |  |  |  | Non-White |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | Dem | $\begin{aligned} & \text { Non- } \\ & \%{ }^{\text {Dem }} \end{aligned}$ | Total | Dem $\qquad$ | $\begin{aligned} & \text { Non- } \\ & \%^{\text {Dem }} \\ & \hline \hline \end{aligned}$ | Total |
| Feel | 42\% | 61\% | 48\% | 40\% | 54\% | 45\% |
| Safer | (15) | (11) | (26) | (8) | (7) | (15) |
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| Total | 100\% (36) | 100\% (18) | 100\% (54) | 100\% (20) | $100 \%$ (13) | $100 \%$ (33) |

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the same size?

- Yes? $\Rightarrow$ additive relationship
- No? $\Rightarrow$ interactive relationship


## BACK TO OUR SURVEY

| White |  |  |  | Non-White |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | Dem | $\begin{aligned} & \text { Non- } \\ & \%{ }^{\text {Dem }} \end{aligned}$ | Total | Dem $\qquad$ | $\begin{aligned} & \text { Non- } \\ & \%^{\text {Dem }} \\ & \hline \hline \end{aligned}$ | Total |
| Feel | 42\% | 61\% | 48\% | 40\% | 54\% | 45\% |
| Safer | (15) | (11) | (26) | (8) | (7) | (15) |
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| Total | 100\% (36) | 100\% (18) | 100\% (54) | 100\% (20) | $100 \%$ (13) | $100 \%$ (33) |

- Partial effect of partisanship, "controlling for" race


## HOW CAN WE TELL WHICH ONE?

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- Yes? $\Rightarrow$ relationship between $x$ and $y$ is spurious
- No? $\Rightarrow$ either additive or interactive

2. Are all controlled/partial effects approximately
the same size?

- Yes? $\Rightarrow$ additive relationship
- No? $\Rightarrow$ interactive relationship

Would also be ok to conclude additive

## INTERACTIVE RELATIONSHIP

## Race (Z)

## Partisanship (X)

## Feeling safer if more armed security (Y)

- Race determines how much of an effect partisanship has on Y
- Partisanship matters among both white and non-white students, but it matters more among white students


## REMEMBER VARIABLE LEVELS

- So far: Dependent variable was nominal-level
- Now: DV is interval level
- e.g. GPA
- We use mean comparison
- Determination if spurious, additive, interactive works just the same


## ZERO-ORDER RELATIONSHIP

## How much sleep during finals?

More Than 6<br>Hours/Night

6 Or Fewer<br>Hours/Night

Average Gpa


- Frequency in parentheses

Number of Classes (Z)

Sleep (X)


- Spurious? Additive? Interactive?


## ZERO-ORDER RELATIONSHIP

## 5 Or Fewer Classes

6 Or More Classes

| Sleep | More Than 6 <br> Hours/Night | 6 Or Fewer <br> Hours/Night | More Than 6 <br> Hours/Night | 6 Or Fewer <br> Hours/Night |
| :---: | :---: | :---: | :---: | :---: |
|  |  |  |  |  |
| Average <br> Gpa | 3.49 | 3.51 | 3.78 | 3.63 |
|  | $(20)$ | $(34)$ | (20) | (18) |

- Frequency in parentheses


## HOW CAN WE TELL WHICH ONE?

1. Are all controlled effects zero or very close to zero?

- Yes? $\Rightarrow$ relationship between x and y is spurious
- No? $\Rightarrow$ either additive or interactive

2. Are all controlled effects approximately the same size?

- Yes? $\Rightarrow$ additive relationship
- No? = interactive relationship


## CONTROLLED EFFECTS

## 5 Or Fewer Classes

6 Or More Classes

Sleep
More Than 6 Or Fewer More Than 6 Or Fewer Hours/Night Hours/Night Hours/Night Hours/Night

Average
Gpa

| 3.49 | 3.51 | 3.78 | 3.63 |
| :---: | :---: | :---: | :---: |
| $(20)-0.02(34)$ | $(20) 0.15$ (18) |  |  |

- Frequency in parentheses


## HOW CAN WE TELL WHICH ONE?

1. Are all controlled effects zero or very close to zero?

- Yes? $\Rightarrow$ relationship between $x$ and $y$ is spurious
- No? $\Rightarrow$ either additive or interactive

2. Are all controlled effects approximately the same size?

- Yes? $\Rightarrow$ additive relationship
- No? = interactive relationship


## CONTROLLED EFFECTS

## 5 Or Fewer Classes

6 Or More Classes

Sleep
More Than 6 Or Fewer More Than 6 Or Fewer Hours/Night Hours/Night Hours/Night Hours/Night

Average
Gpa

| 3.49 | 3.51 | 3.78 | 3.63 |
| :---: | :---: | :---: | :---: |
| $(20)-0.02(34)$ | $(20) 0.15$ (18) |  |  |

- Frequency in parentheses


## HOW CAN WE TELL WHICH ONE?

1. Are all controlled effects zero or very close to zero?

- Yes? $\Rightarrow$ relationship between x and y is spurious
- No? $\Rightarrow$ either additive or interactive

2. Are all controlled effects approximately the same size?

- Yes? $\Rightarrow$ additive relationship
- No? $\Rightarrow$ interactive relationship


## Sleep (X)



## GPA

- Number of classes determines how much sleep affects

GPA

- Sleep matters quite a bit among students who take 6 or more classes
- Sleep doesn't matter as much for students who take 5 or fewer classes


## A REAL-WORLD EXAMPLE

- 2020 Presidential election: Joe Biden (D) vs. Donald Trump (R)
- Hypothesis: People with a college degree were more likely to vote for Joe Biden than people without a college degree

Education (X)


Voting for Biden (Y)

The Alew llork Times
National Exit Polls: How Different Groups Voted


Joseph R. Biden Jr.
What is your level of education?
College graduate
41\% of voters
No college degree
59\%

| 43 | 55 |
| :---: | :---: |
| 50 | 48 |

## ZERO-ORDER RELATIONSHIP

## Education

College Degree

No College
Degree

Biden Vote Share

| $55 \%$ |  |
| :--- | :--- |
|  | $7 \%$ |
|  |  |

## VOTING FOR BIDEN

## Race/Ethnicity (Z)




Voting for Biden (Y)

- Is relation between $X$ and $Y$ spurious? Additive? Interactive?


## RACE AND EDUCATION



Joseph R. Biden Jr.

## What is your race and education level?

White college graduate
$32 \%$ of voters
White noncollege graduate 35\%

Nonwhite college graduate 10\%

Nonwhite noncollege graduate
26
51

32

24\%

| 48 | 51 |
| :---: | :---: |
| 67 | 32 |
| 27 | 70 |
| 26 | 72 |

## CONTROLLED EFFECTS

## White

## Nonwhite



## HOW CAN WE TELL WHICH ONE?

1. Are all controlled effects zero or very close to zero?

- Yes? $\Rightarrow$ relationship between x and y is spurious
- No? $\Rightarrow$ either additive or interactive

2. Are all controlled effects approximately the same size?

- Yes? $\Rightarrow$ additive relationship
- No? = interactive relationship


## VOTING FOR BIDEN

## Race/Ethnicity (Z)

Education (X)


Voting for Biden (Y)

- Education matters a lot among white voters
- Education does not matter among nonwhite voters


## AFTER THE BREAK

- How to do controlled effects in a linear regression
- What to do if there is more than one confounder?

